

بسم الله الرحمن الرحيم

Week No.	Section	Topics	Problems
1	1.9	Vectors	(Example 1.12, Page 20) +
	1.10	Components of Vector	Tutorial Problems

TEXTBOOK:

College Physics, 11 edition By Raymond A. Serway, Chris Vuille, CENGAGE, 2018, ISBN: 978-1-337-62033-8

المتجهات Vectors

قياسية

Scalar

→ magnitude only
المقدار فقط

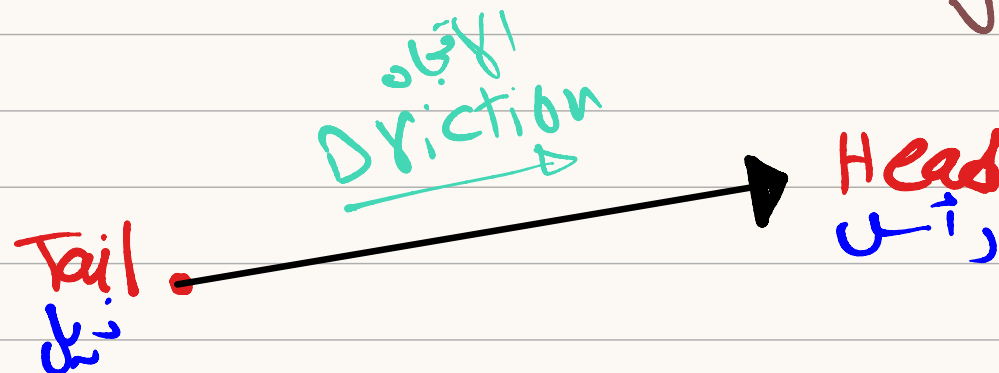
EX: mass
Temp

متجهة

Vector

→ magnitude
→ Direction
المقدار والاتجاه

EX: Force \leftrightarrow \updownarrow
velocity



1.9 Vectors المتجهات

قياس

- **Scalar quantity**, can be completely described by a **single number** (with appropriate units) giving its **magnitude or size**. مقدار

e.g., mass, temperature, volume, and speed.

السرعة القياسية الحجم د.ق الحرارة الكتلة اتجاه

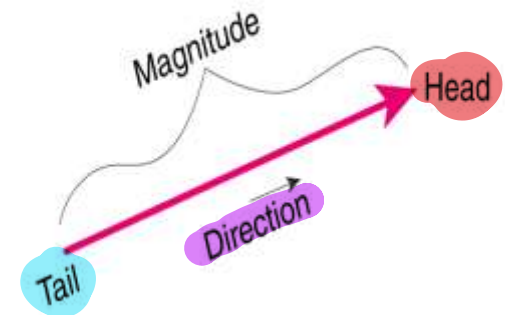
- **Vector quantity**, has both a **magnitude and a direction**.

e.g., velocity, acceleration and force

عقدار و اتجاه القوة العجل سرعة متجهة

Representation of vectors:

- A vector quantity is often represented with bold face type with an arrow over the letter (\vec{A})
- The magnitude of the vector will be represented by italic type, as A .
- Italic type will also be used to represent scalars



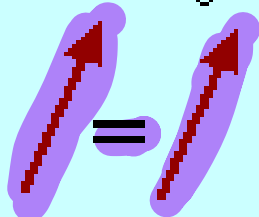
1.9.1 Equality of Two Vectors

نفس الاتجاه نفس المقدار

- Two vectors are equal if they have the same magnitude and the same direction.
- Any vector can be moved parallel to itself without being affected.

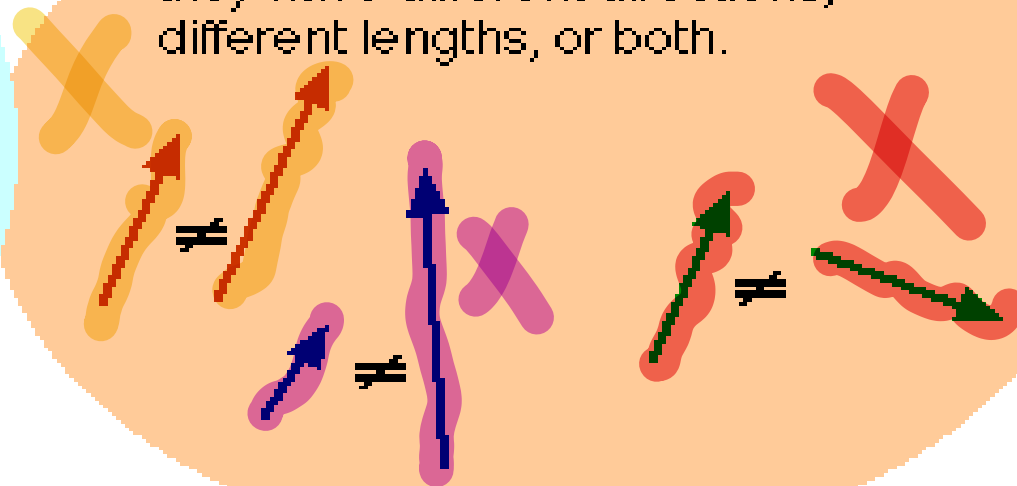
موازي

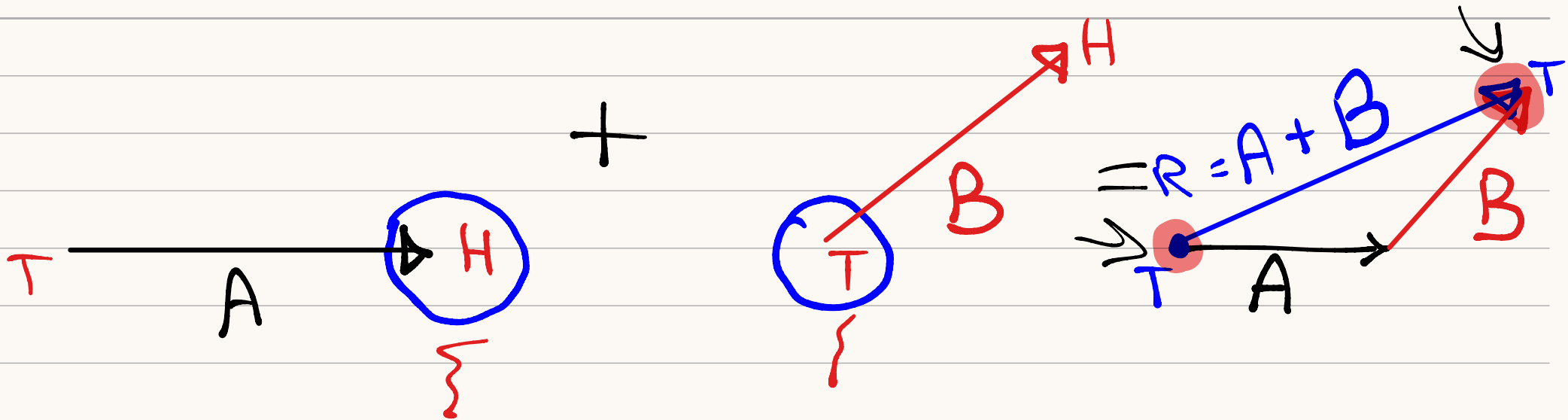
Equal Vectors have the same directions and lengths



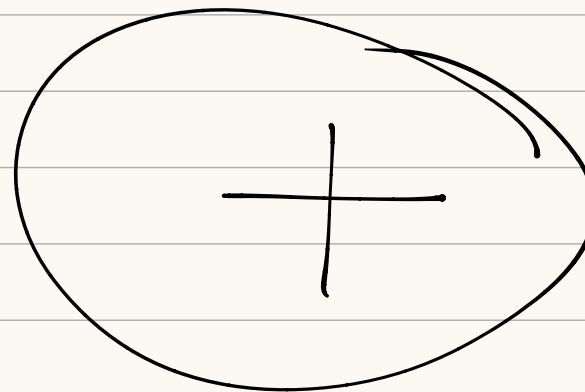
But they may be in different places.

Vectors may be unequal because they have different directions, different lengths, or both.



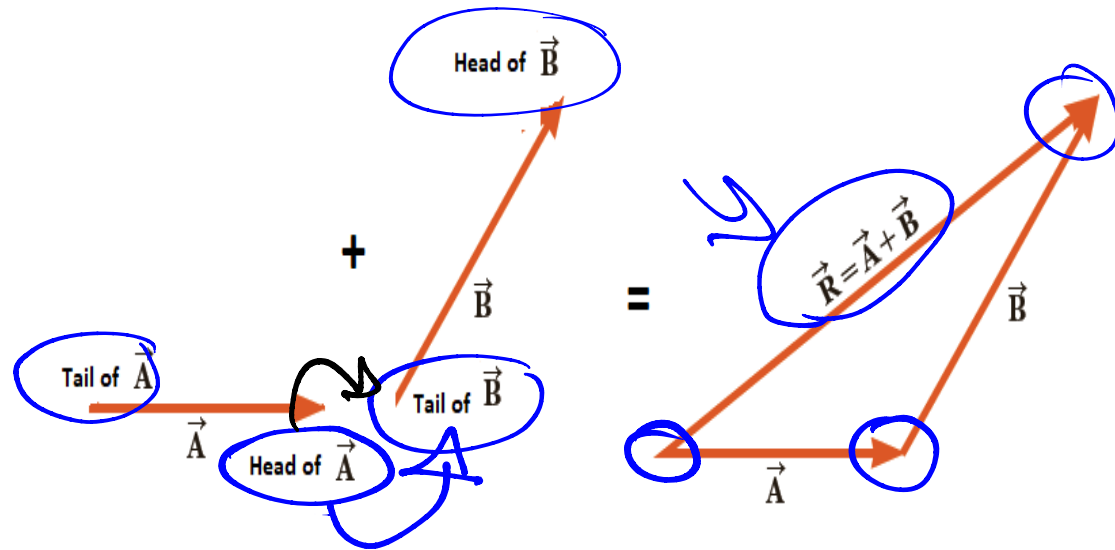


Resultant $\leftarrow R = A + B = B + A$



1.9.2 Adding Vectors

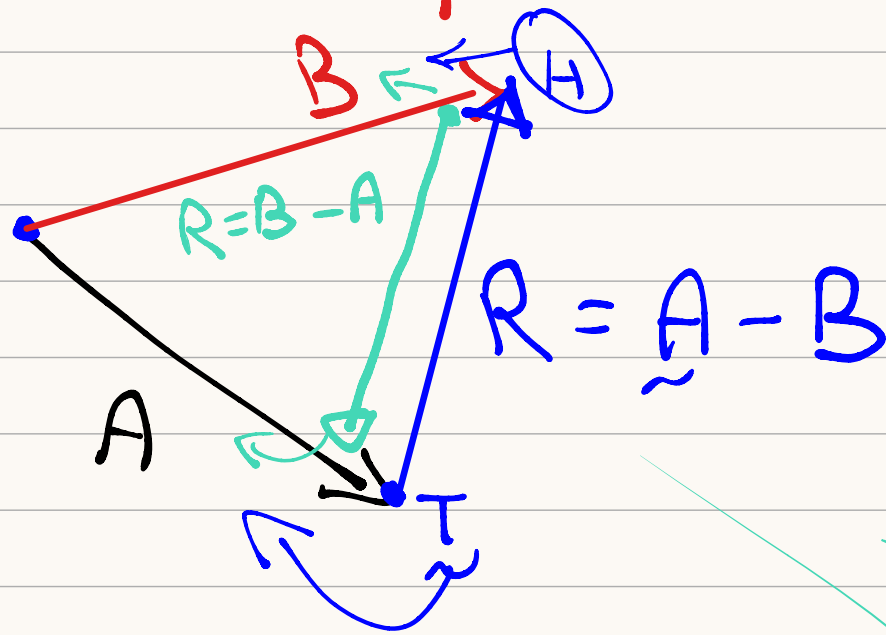
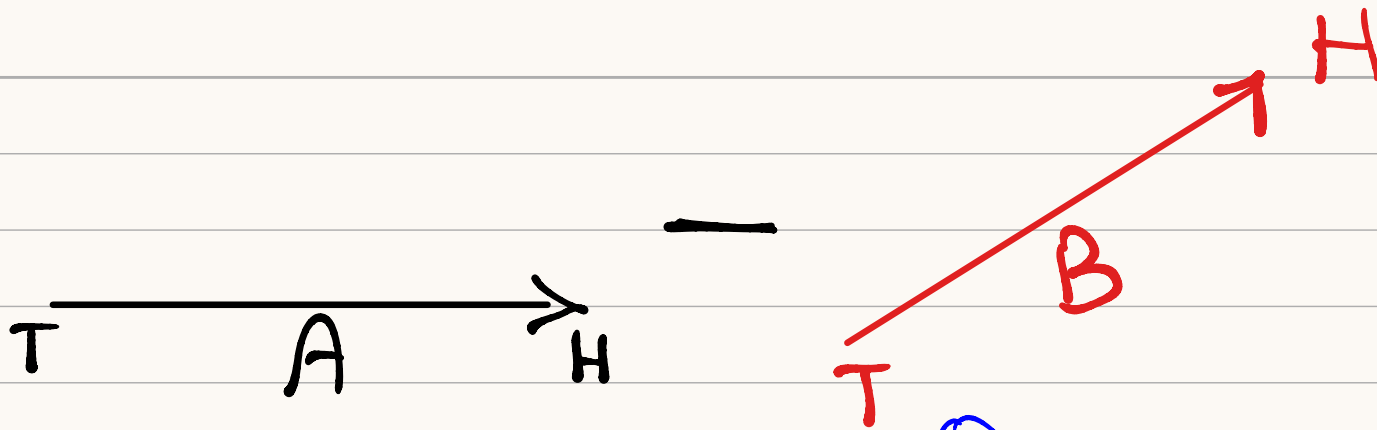
- Draw the first vector (\vec{A}), then place the tail of the second vector (\vec{B}) at the head of the first.
- Finally draw the resultant ($\vec{R} = \vec{A} + \vec{B}$) from the tail of \vec{A} to the head of \vec{B} to complete the triangle



➤ This procedure is known as the **triangle method of addition**.

➤ When two vectors are added, their sum is independent of the order of the addition. $\vec{A} + \vec{B} = \vec{B} + \vec{A}$ is called the **commutative law of addition**.

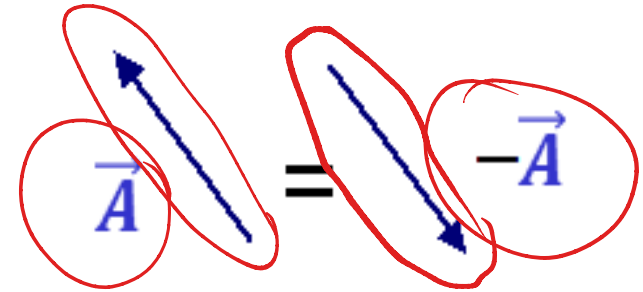
علاقہ ابوالہیہ



قواعد
الطريق

1.9.3 Negative of a vector:

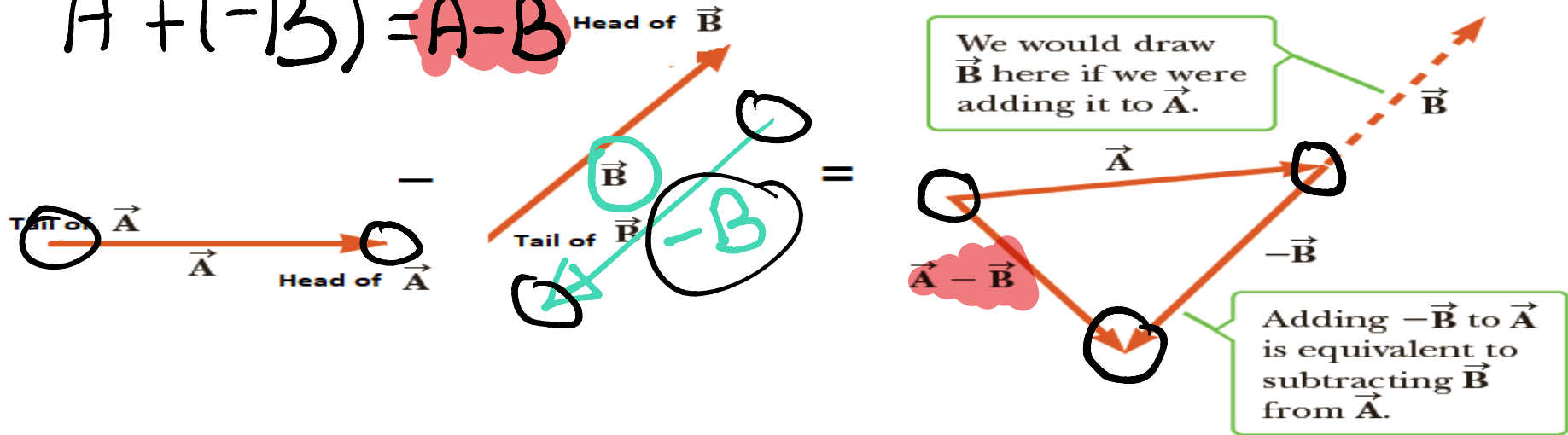
A vector with the **same magnitude** (length) but pointing in the **exact opposite direction**.
نفس المقدار
عكس الاتجاه



1.9.4 subtracting Vectors

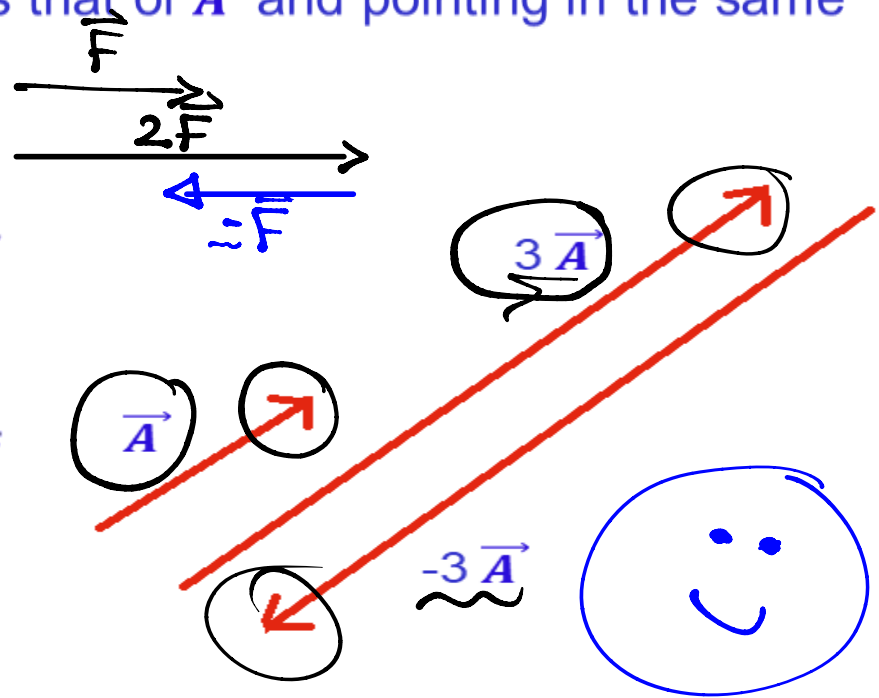
- Vector subtraction makes use of the definition of the negative of a vector.
- The operation $\vec{A} - \vec{B} = \vec{A} + (-\vec{B})$ is the vector $-\vec{B}$ added to the vector \vec{A}

$$A + (-B) = A - B$$

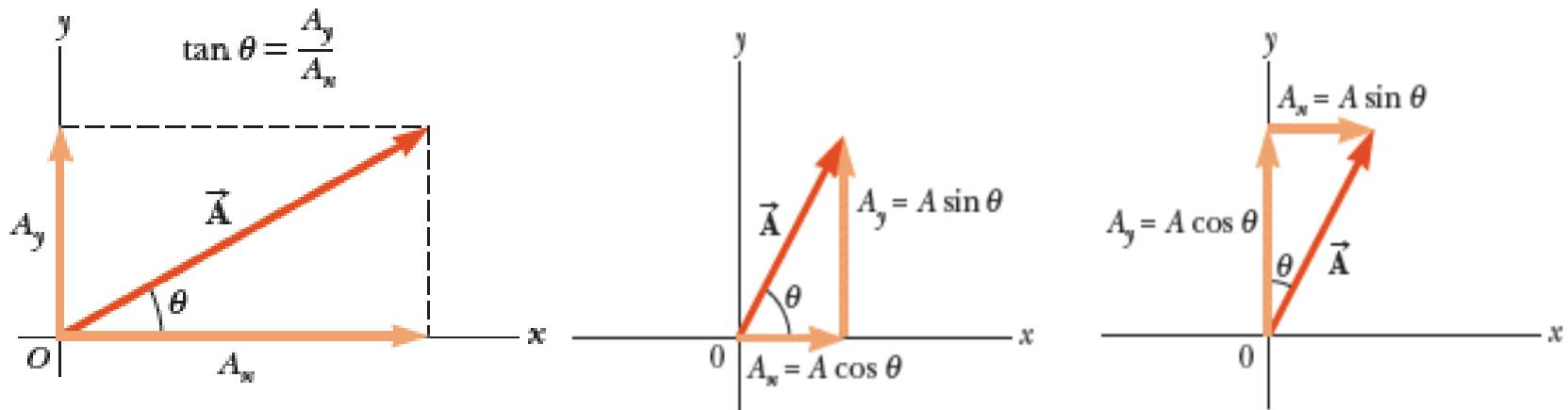


1.9.5 Multiplying or dividing a Vector by a scalar

- Multiplying or dividing a vector by a scalar gives a vector.
- If vector \vec{A} is multiplied by the scalar number 3, the result, written $3\vec{A}$ is a vector with a magnitude three times that of \vec{A} and pointing in the same direction.
- If we multiply vector \vec{A} by the scalar -3, the result is $-3\vec{A}$, a vector with a magnitude three times that of \vec{A} and pointing in the opposite direction (because of the negative sign).



1.10 Components of a Vector



- To add vectors makes use of the projections of a vector along the axes.
- These projections are called components.

From Fig. we have,

Also we have, $\vec{A} = \vec{A}_x + \vec{A}_y$

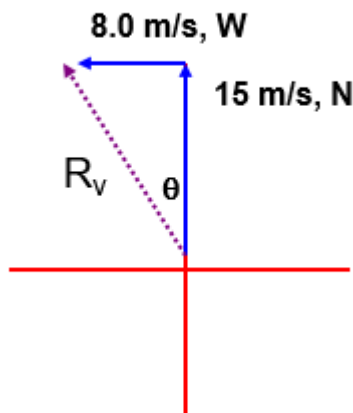
$$A_x = A \cos \theta$$

$$A_y = A \sin \theta$$

$$A = \sqrt{A_x^2 + A_y^2}$$

$$\tan \theta = \frac{A_y}{A_x} \quad \theta = \tan^{-1} \left(\frac{A_y}{A_x} \right)$$

Example: A boat moves with a velocity of 15 m/s, N in a river which flows with a velocity of 8.0 m/s, west. Calculate the boat's resultant velocity with respect to due north.



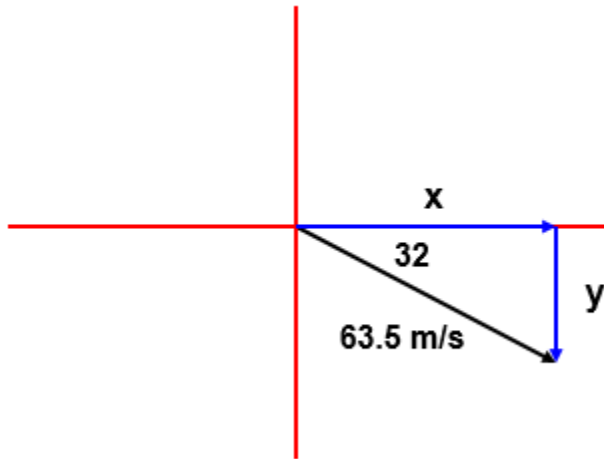
$$R_v = \sqrt{8^2 + 15^2} = 17 \text{ m/s}$$

$$\tan \theta = \frac{8}{15} = 0.5333$$

$$\theta = \tan^{-1}(0.5333) = 28.1^\circ$$

The Final Answer : **17 m/s, @ 28.1 degrees West of North**

Example : A plane moves with a velocity of 63.5 m/s at 32 degrees South of East. Calculate the plane's horizontal and vertical velocity components.



$$\begin{aligned}A_x &= A \cos \theta \\&= (63.5)\cos 32 \\&= 53.85 \text{ m/s , east}\end{aligned}$$

$$\begin{aligned}A_y &= A \sin \theta \\&= (63.5)\sin 32 \\&= 33.64 \text{ m/s , south}\end{aligned}$$

